

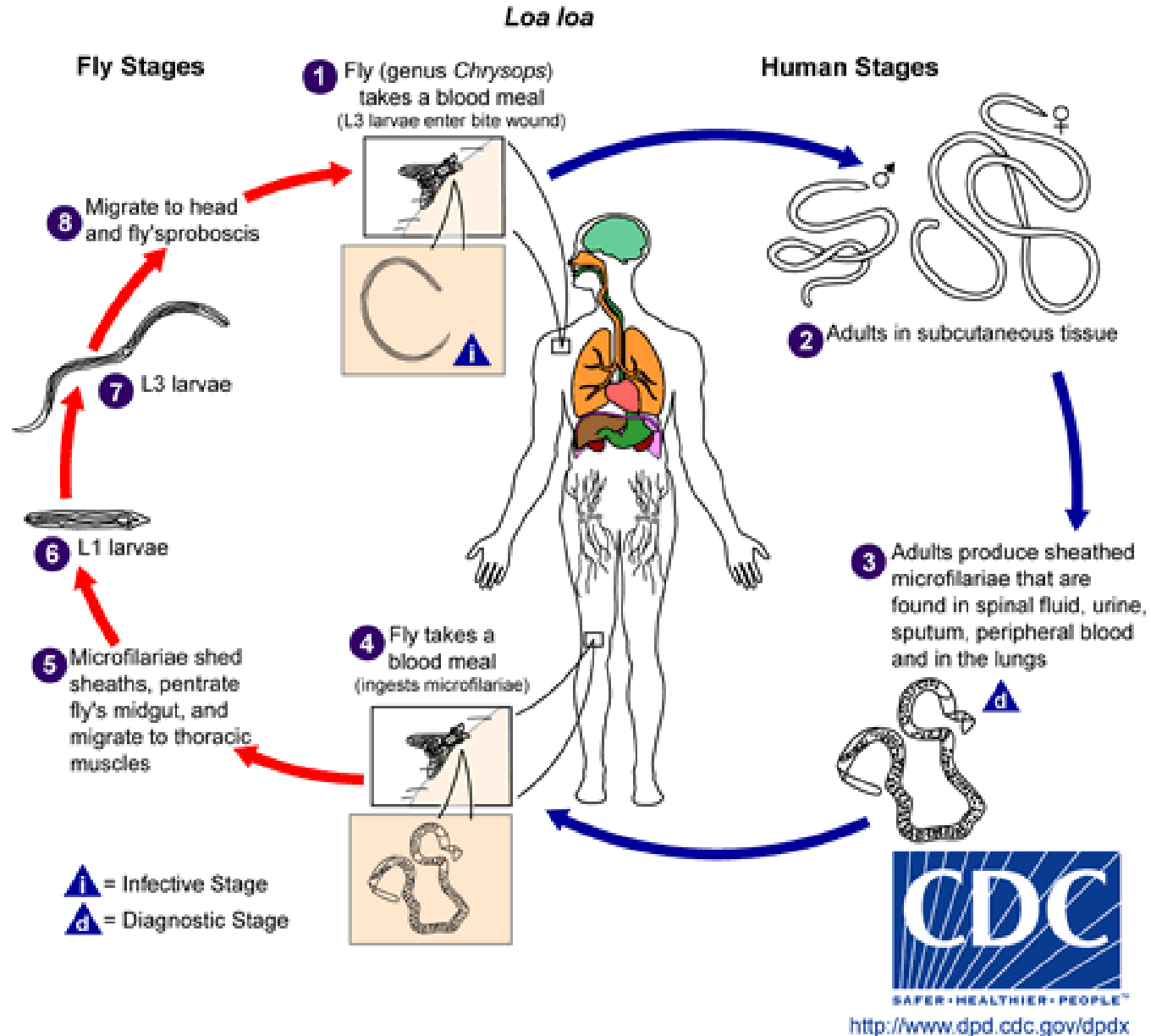
# Point referenced data (pt. 2)

Lecture 22

Dr. Colin Rundel

# Loa Loa Example

# Loa Loa



# Data

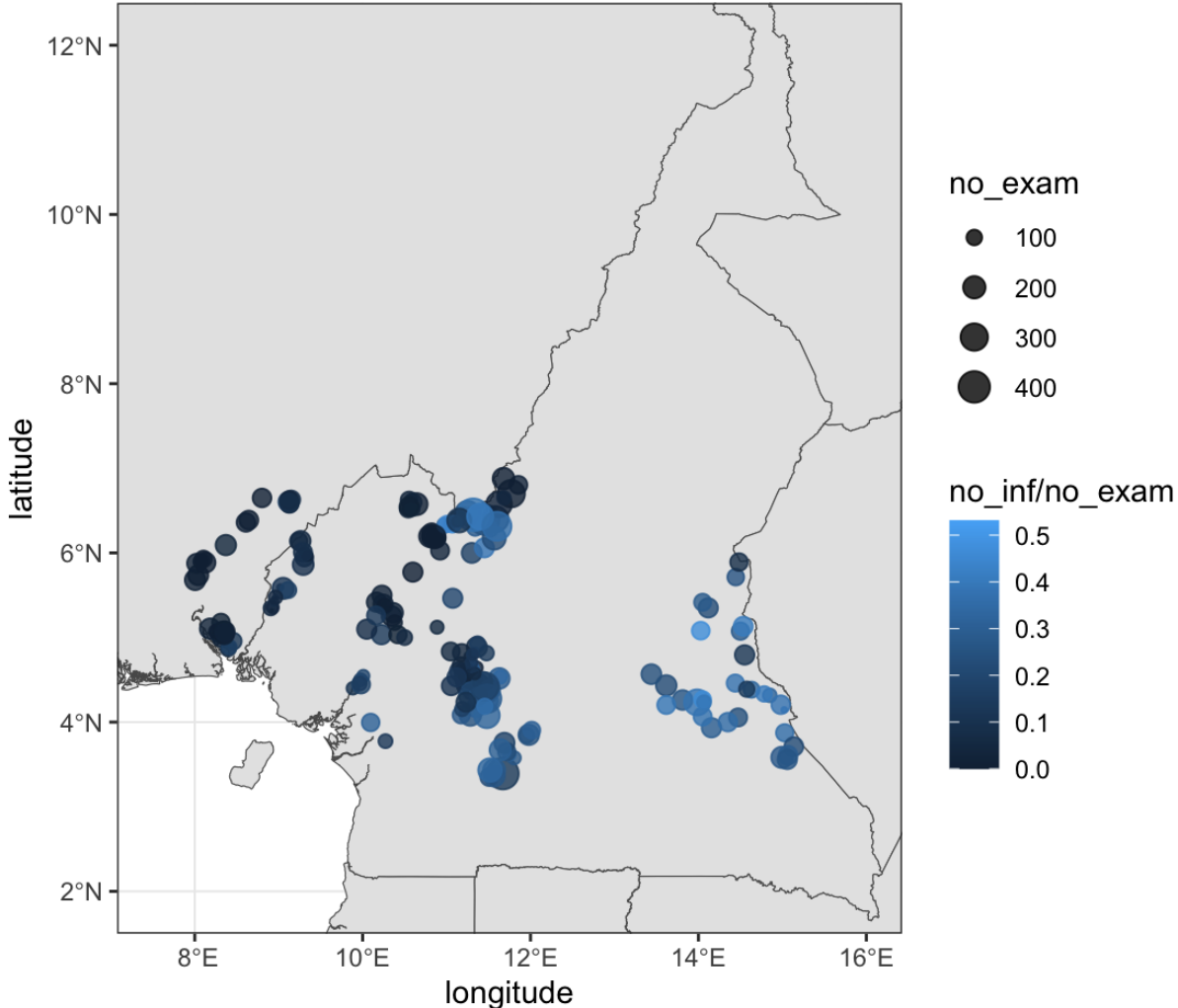
```
1 loaloe = PrevMap::loaloe %>%
2   as_tibble() %>%
3   setNames(., tolower(names(.))) %>%
4   rename(elev=elevation)
5
6 loaloe
```

```
# A tibble: 197 × 11
```

```
   row villcode longi...1 latit...2 no_exam no_inf elev mean9...3 max9901
  <int>   <int>   <dbl>   <dbl>   <int>   <int> <int>   <dbl>   <dbl>
1     1     214    8.04    5.74    162     0   108    0.439    0.69
2     2     215    8.00    5.68    167     1    99    0.426    0.74
3     3     118    8.91    5.35     88     5   783    0.491    0.79
4     4     219    8.10    5.92     62     5   104    0.432    0.67
5     5     212    8.18    5.10    167     3   109    0.415    0.85
6     6     116    8.93    5.36     66     3   909    0.436    0.8
7     7      16   11.4    4.88    163    11   503    0.502    0.78
8     8     217    8.07    5.90     83     0   103    0.373    0.69
9     9     112    9.02    5.59     30     4   751    0.481    0.8
10    10     104    9.31    6.00     57     4   268    0.487    0.84
```

```
# ... with 187 more rows, 2 more variables: min9901 <dbl>,
#   stdev9901 <dbl>, and abbreviated variable names 1longitude,
#   2latitude. 3mean9901
```

# Spatial Distribution



# Normalized Difference Vegetation Index (NDVI)

# Paper / Data summary

Original paper - Diggle, et. al. (2007). *Spatial modelling and prediction of *Loa loa* risk: decision making under uncertainty*. *Annals of Tropical Medicine and Parasitology*, 101, 499-509.

- `no_exam` and `no_inf` - Collected between 1991 and 2001 by NGOs (original paper mentions 168 villages and 21,938 observations)
- `elev` - USGS gtopo30 (1km resolution)
- `mean9901` to `stdev9901` - aggregated data from 1999 to 2001 from the Flemish Institute for Technological Research (1 km resolution)

# Diggle's Model

$$\begin{aligned}\log\left(\frac{p(s)}{1-p(s)}\right) &= \alpha + f_1(\text{elev}(s)) \\ &+ f_2(\text{MAX.NDVI}(s)) \\ &+ f_3(\text{SD.NDVI}(s)) + w(s)\end{aligned}$$

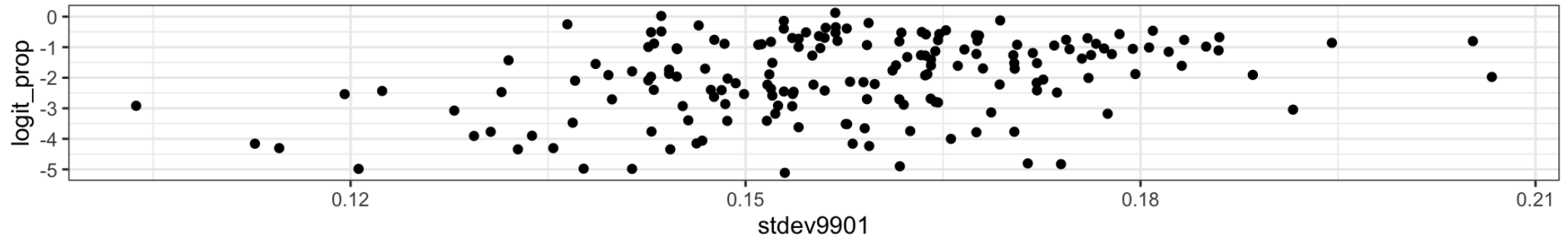
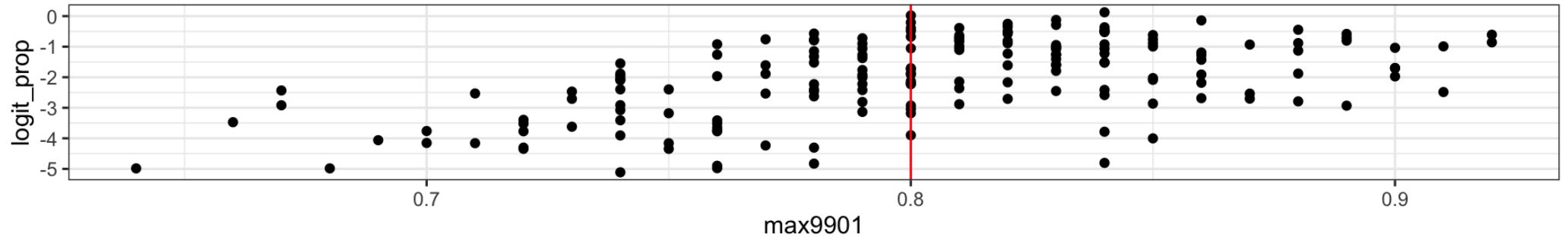
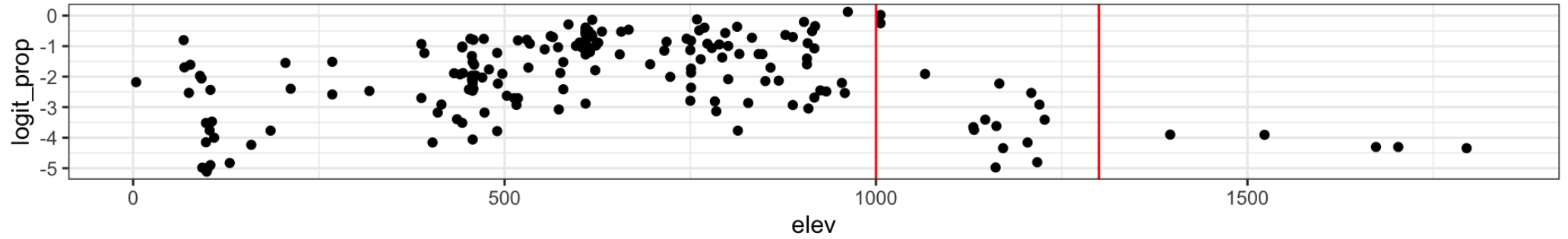
where

$$w(s) \sim (0, \Sigma)$$

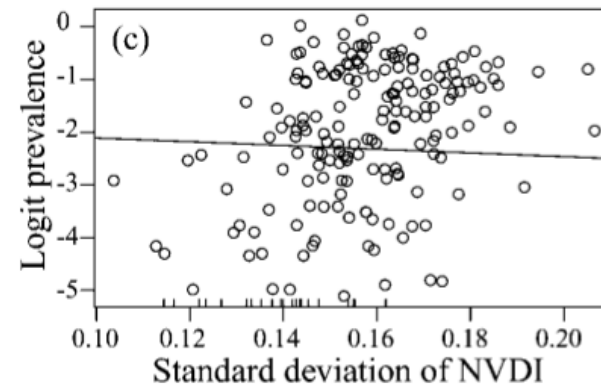
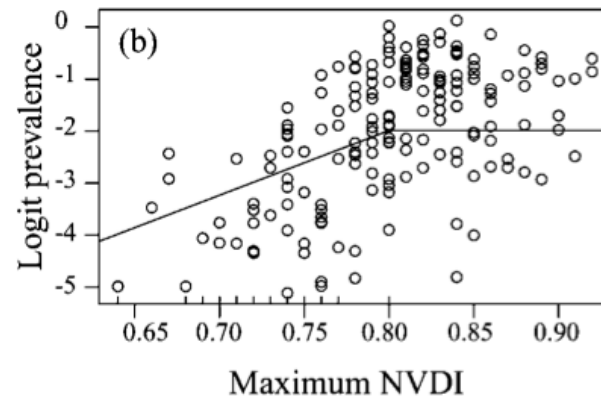
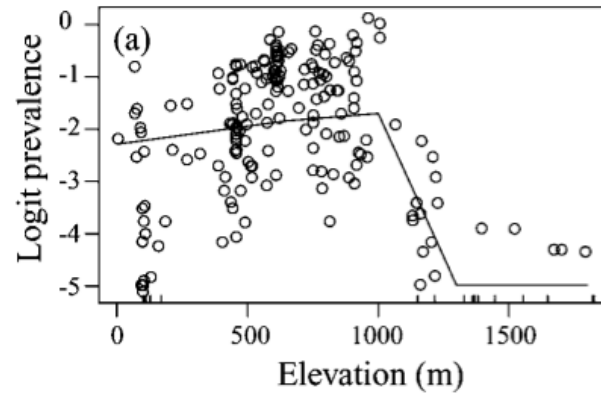
$$\{\Sigma\}_{ij} = \sigma^2 \exp(-d \phi)$$



# EDA



# Diggle's EDA



# Feature engineering

```
1 loaloe = loaloe %>%
2   mutate(
3     elev_f = cut(elev, breaks=c(0,1000,1300,2000), dig.lab=5),
4     max_f  = cut(max9901, breaks=c(0,0.8,1))
5   )
6 loaloe %>% select(elev, elev_f, max9901, max_f)
```

```
# A tibble: 197 × 4
```

	elev	elev_f	max9901	max_f
	<int>	<fct>	<dbl>	<fct>
1	108	(0,1000]	0.69	(0,0.8]
2	99	(0,1000]	0.74	(0,0.8]
3	783	(0,1000]	0.79	(0,0.8]
4	104	(0,1000]	0.67	(0,0.8]
5	109	(0,1000]	0.85	(0.8,1]
6	909	(0,1000]	0.8	(0,0.8]
7	503	(0,1000]	0.78	(0,0.8]
8	103	(0,1000]	0.69	(0,0.8]
9	751	(0,1000]	0.8	(0,0.8]
10	268	(0,1000]	0.84	(0.8,1]

```
# ... with 187 more rows
```

# Model Matrix

```
1 model.matrix(  
2   ~ elev:elev_f - 1,  
3   data = loaloa  
4 ) %>%  
5   as_tibble()
```

```
# A tibble: 197 × 3
```

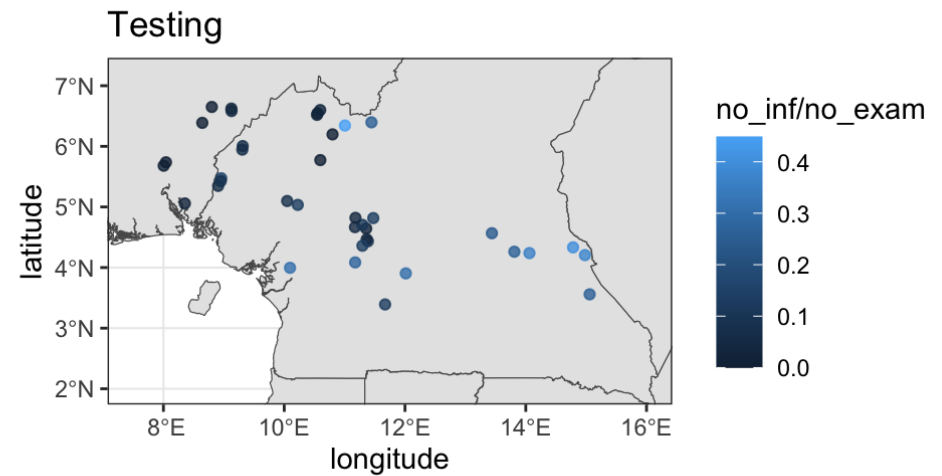
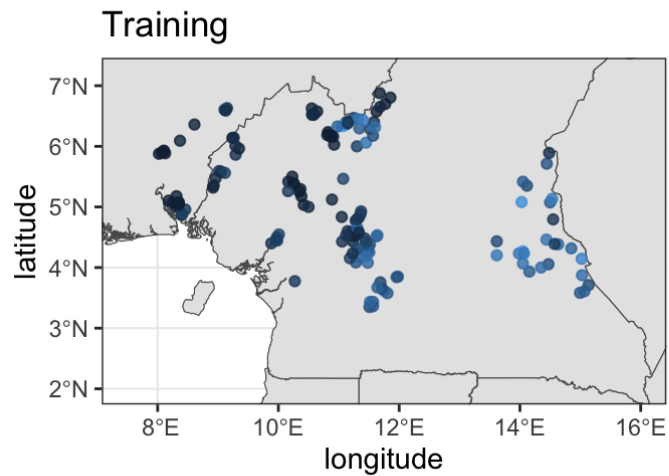
```
  `elev:elev_f(0,1000]` `elev:elev_f(1000,1300]` elev:elev_f(1300,2...1  
    <dbl>                <dbl>                <dbl>  
1         108                0                0  
2          99                0                0  
3        783                0                0  
4        104                0                0  
5        109                0                0  
6       909                0                0  
7        503                0                0  
8        103                0                0  
9       751                0                0  
10       268                0                0
```

```
# ... with 187 more rows, and abbreviated variable name
```

```
#   1`elev:elev_f(1300,2000]`
```

# OOS Validation

```
1 set.seed(12345)
2 loaloa_test = loaloa %>% slice_sample(prop=0.20)
3 loaloa = anti_join(loaloa, loaloa_test, quiet=TRUE)
```



# Model

```
1 g = glm(no_inf/no_exam ~ elev:elev_f + max9901:max_f + stdev9901,  
2       data=loaloe, family=binomial, weights=loaloe$no_exam)  
3 summary(g)
```

Call:

```
glm(formula = no_inf/no_exam ~ elev:elev_f + max9901:max_f +  
     stdev9901, family = binomial, data = loaloe, weights = loaloe$no_exam)
```

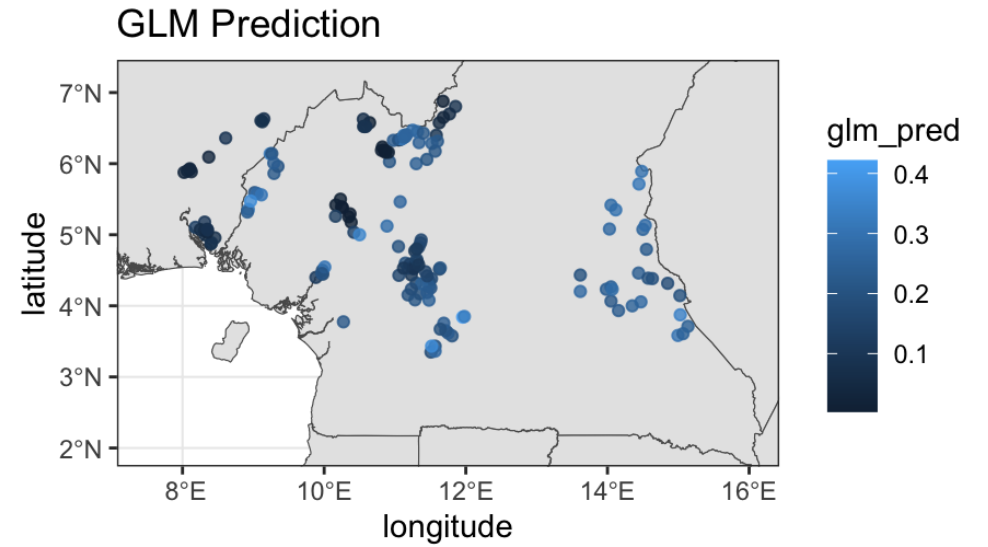
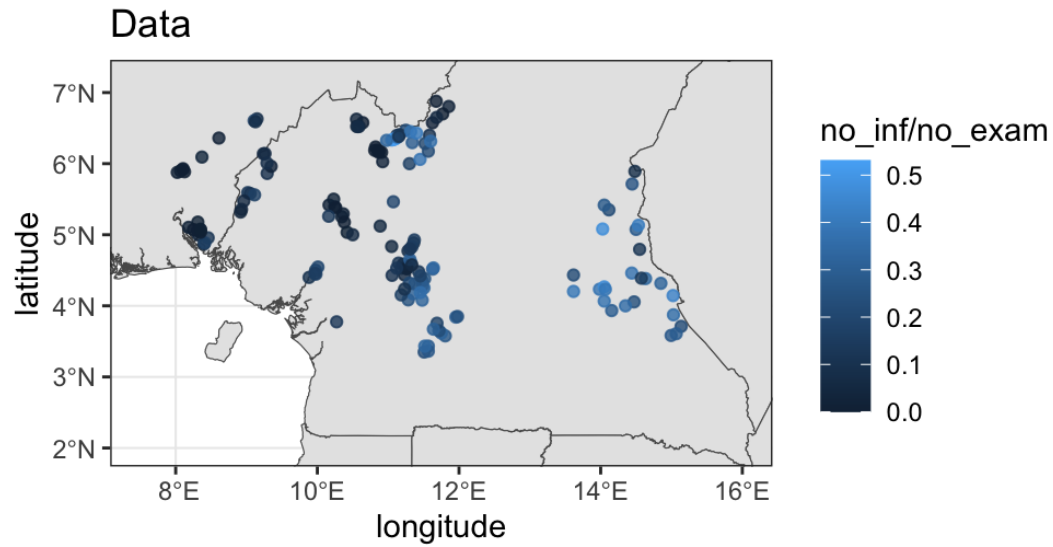
Deviance Residuals:

Min	1Q	Median	3Q	Max
-7.2205	-2.4954	-0.7776	1.6020	9.9667

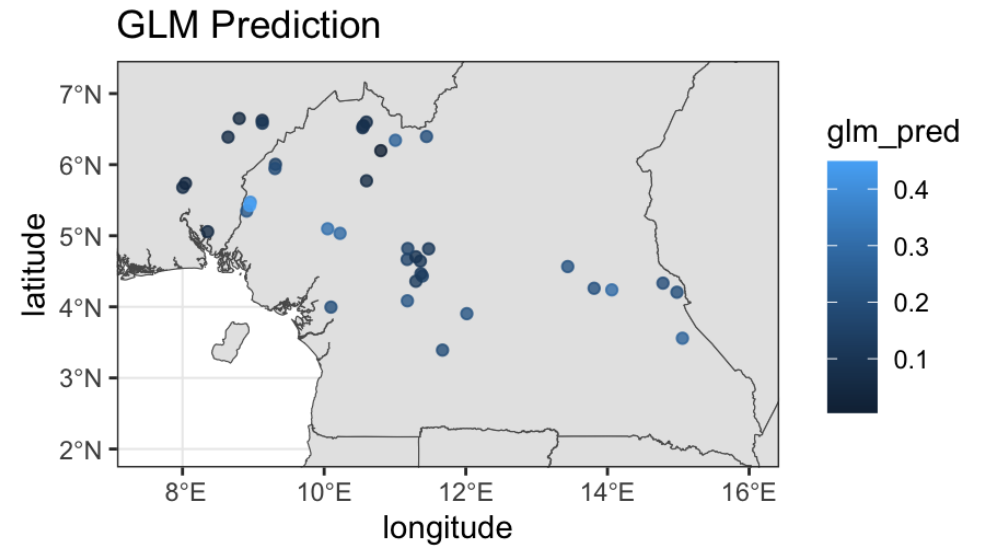
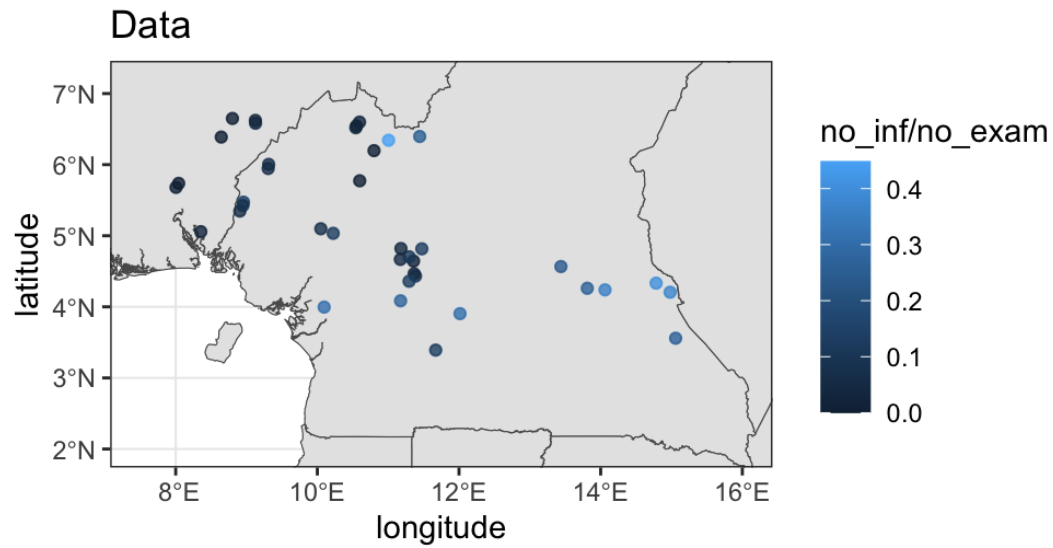
Coefficients:

	Estimate	Std. Error	z value	Pr(> z )	
(Intercept)	-8.537e+00	5.408e-01	-15.785	< 2e-16	***
stdev9901	6.750e+00	1.449e+00	4.659	3.18e-06	***
elev:elev_f(0,1000]	1.467e-03	9.481e-05	15.471	< 2e-16	***
elev:elev_f(1000,1300]	1.940e-04	9.279e-05	2.091	0.0365	*
elev:elev_f(1300,2000]	-1.506e-03	1.912e-04	-7.880	3.29e-15	***

# Predictions - Training

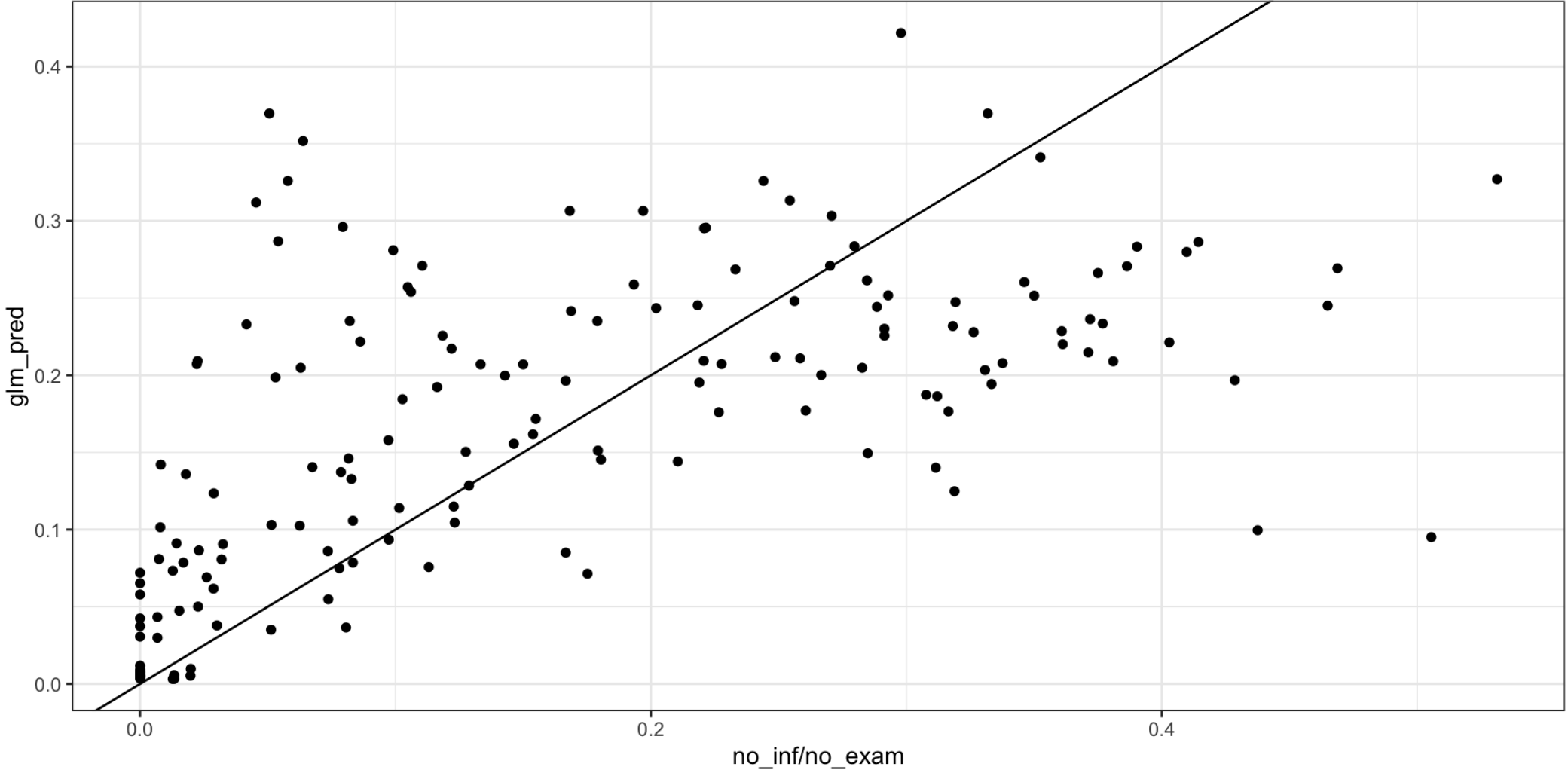


# Predictions - Testing

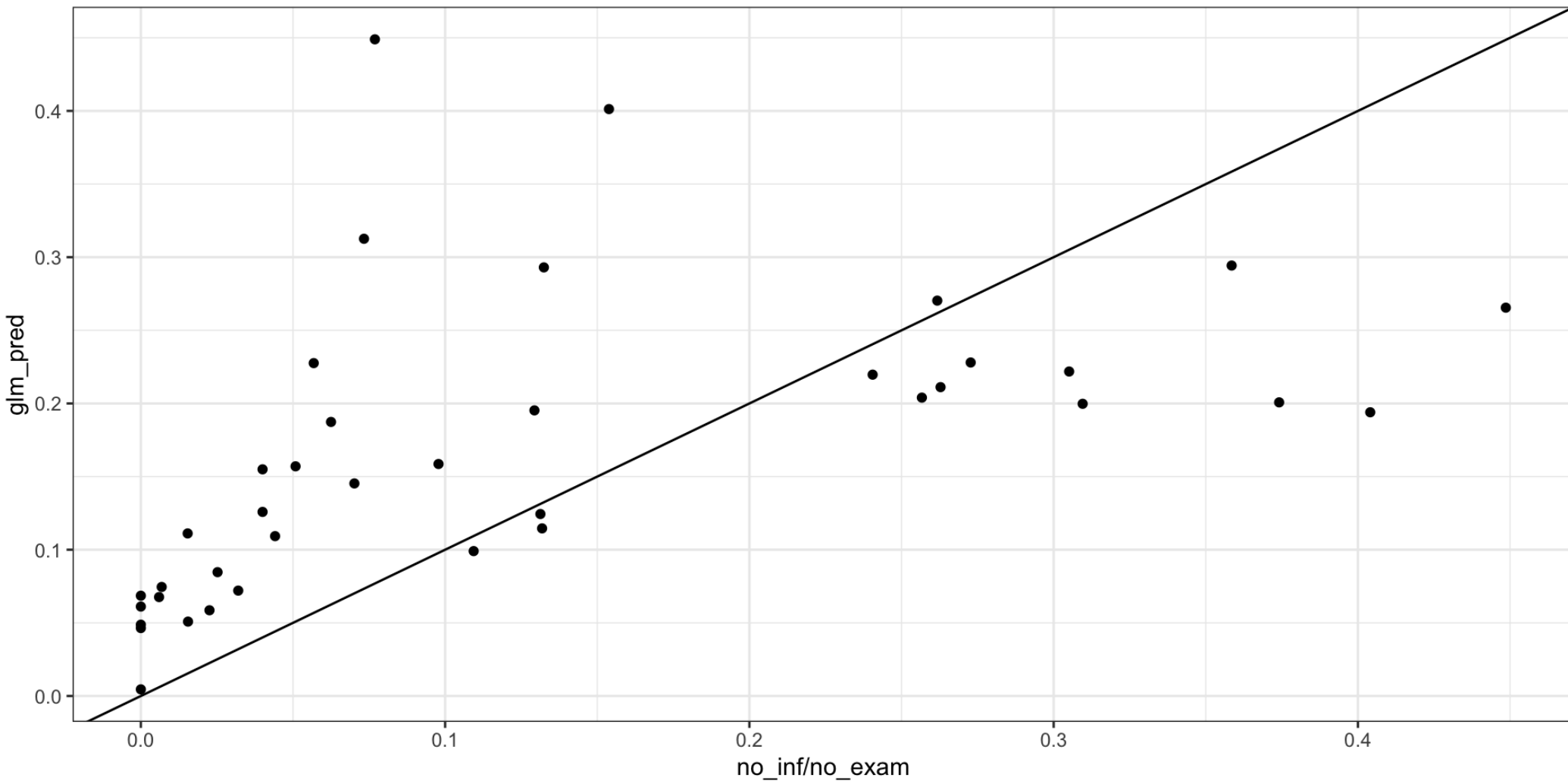




# Fit - Training



# Fit - Testing



# Fit - RMSE

```
1 # Training
2 yardstick::rmse_vec(loaloe$no_inf/loaloe$no_exam, loaloe$glm_pred)
```

```
[1] 0.11176
```

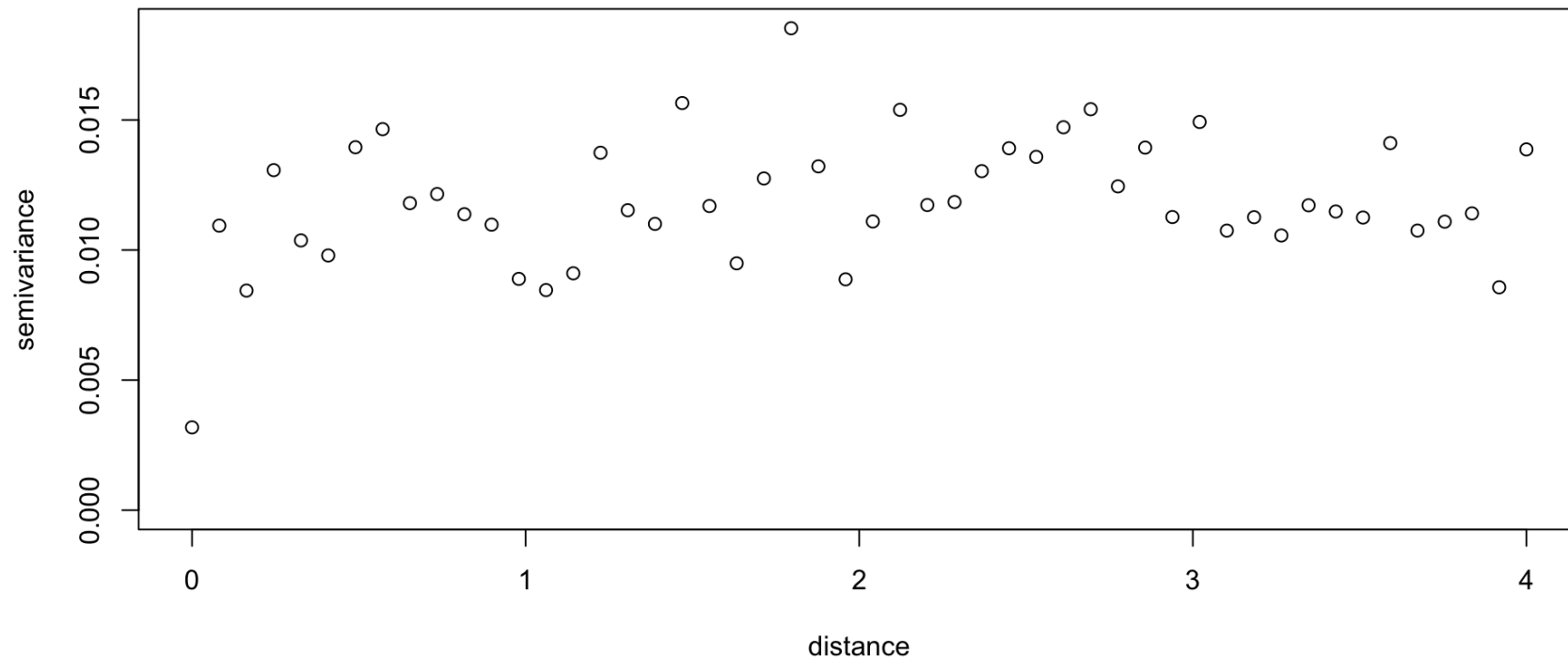
```
1 # Testing
2 yardstick::rmse_vec(loaloe_test$no_inf/loaloe_test$no_exam, loaloe_test$
```

```
[1] 0.1192507
```

# Spatial Structure?

```
1 geoR::variog(coords = cbind(loaloe$longitude, loaloe$latitude),  
2     data = loaloe$prop - loaloe$glm_pred,  
3     uvec = seq(0, 4, length.out = 50)) %>% plot()
```

variog: computing omnidirectional variogram



# gpglm model

```
1 ll_gp = gpglm(  
2   no_inf ~ scale(elev):elev_f + scale(max9901):max_f + scale(stdev9901),  
3   data = loaloe, family="binomial", weights=loaloe$no_exam,  
4   coords = c("longitude", "latitude"),  
5   cov_model="exponential",  
6   starting = list(  
7     beta=rep(0,7),  
8     phi=3, sigma.sq=1, w=0  
9   ),  
10  priors = list(  
11    beta.Normal=list(rep(0,7), rep(10,7)),  
12    phi.unif=c(3/4, 3/0.25), sigma.sq.ig=c(2, 2)  
13  ),  
14  tuning = list(  
15    "beta"=rep(0.1, 7),  
16    "phi"=0.6, "sigma.sq"=0.3, "w"=0.1  
17  ),  
18  n_batch = 400,  
19  batch_len = 50,  
20  verbose = TRUE,  
21  n_report = 10,  
22  chains=4
```

```
1 ll_gp
```

```
# A gpglm model (spBayes spGLM) with 4 chains, 9 variables, and 80000 iterations.
```

```
# A tibble: 9 × 10
```

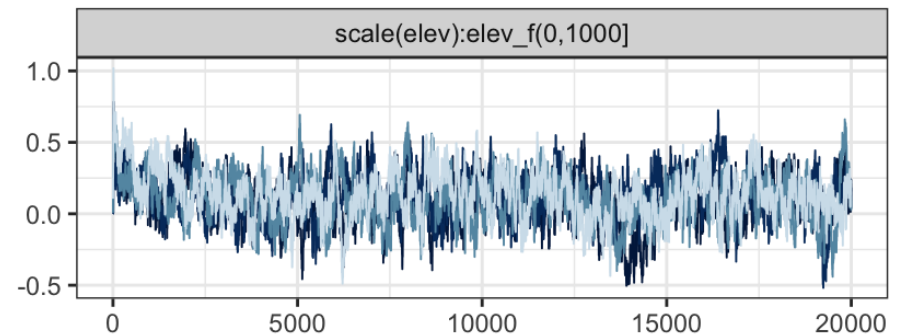
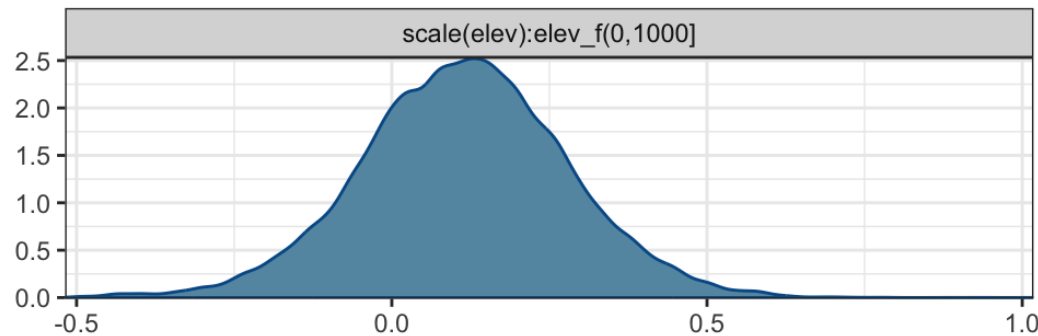
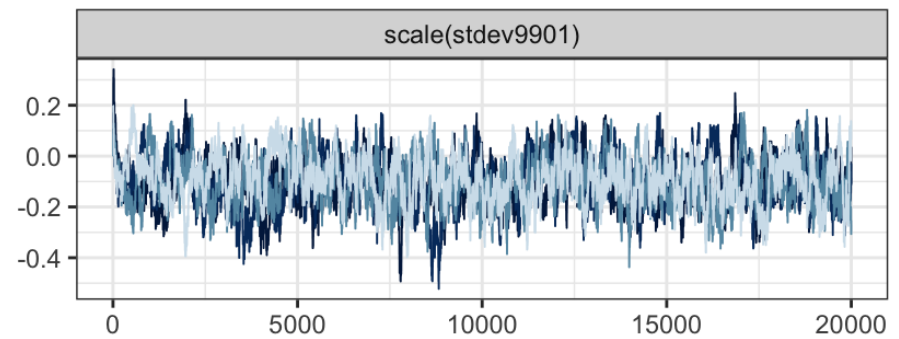
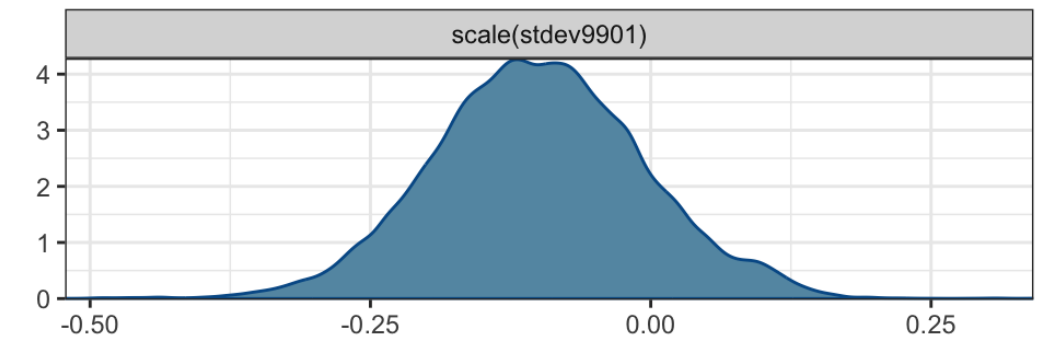
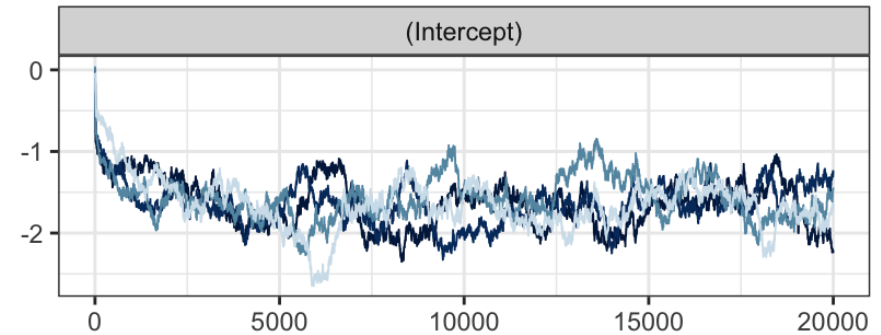
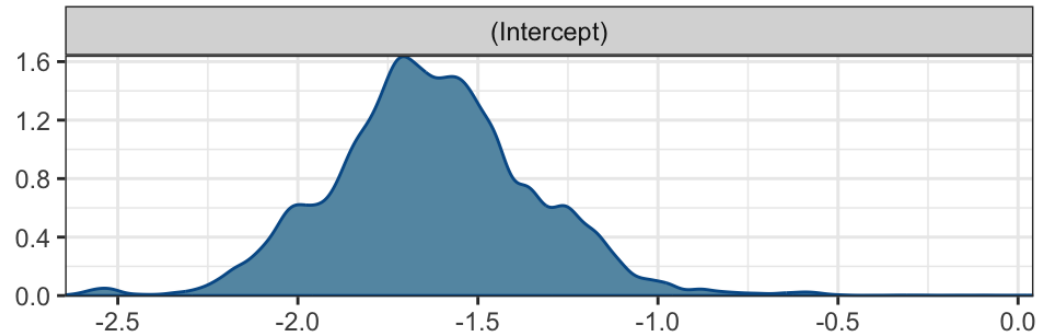
variable	mean	median	sd	mad	q5	q95	rhat	ess_b... <sup>1</sup>
<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1 (Intercept)	-1.63	-1.64	0.282	0.254	-2.07	-1.17	1.03	68.4
2 scale(stde...	-0.100	-0.101	0.0943	0.0930	-0.253	0.0587	1.01	451.
3 scale(elev...	0.114	0.115	0.164	0.159	-0.156	0.383	1.01	225.
4 scale(elev...	-0.800	-0.803	0.283	0.278	-1.26	-0.328	1.02	318.
5 scale(elev...	-1.50	-1.50	0.264	0.261	-1.93	-1.07	1.01	359.
6 scale(max9...	0.718	0.717	0.182	0.179	0.419	1.02	1.01	473.
7 scale(max9...	0.100	0.100	0.150	0.148	-0.142	0.346	1.01	265.
8 sigma.sq	1.04	0.982	0.300	0.237	0.683	1.57	1.01	521.
9 phi	3.08	2.95	1.03	0.935	1.63	4.94	1.01	445.

```
# ... with 1 more variable: ess_tail <dbl>, and abbreviated variable
```

```
# name 'ess_bulk'
```

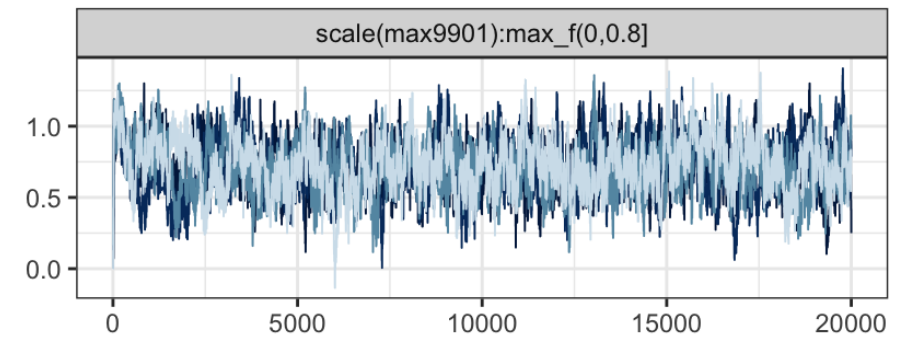
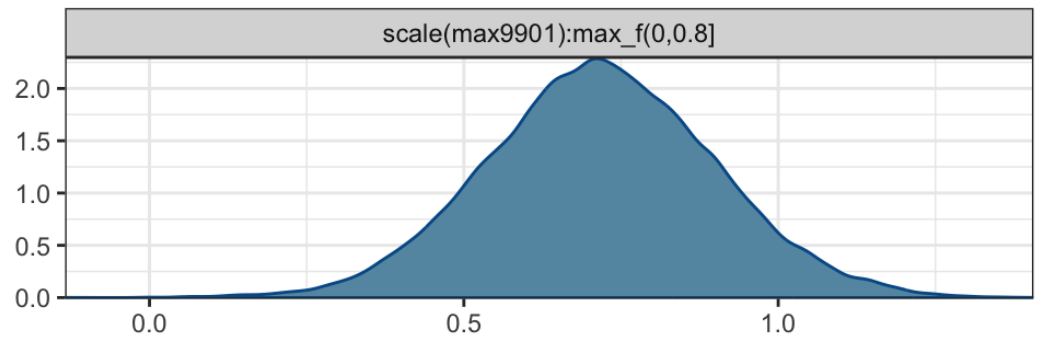
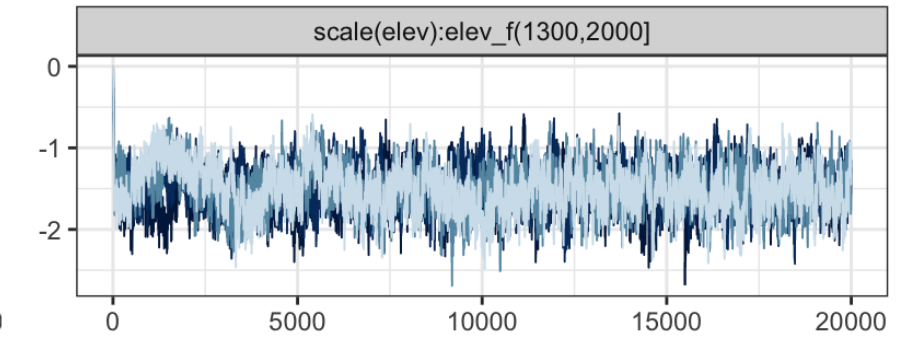
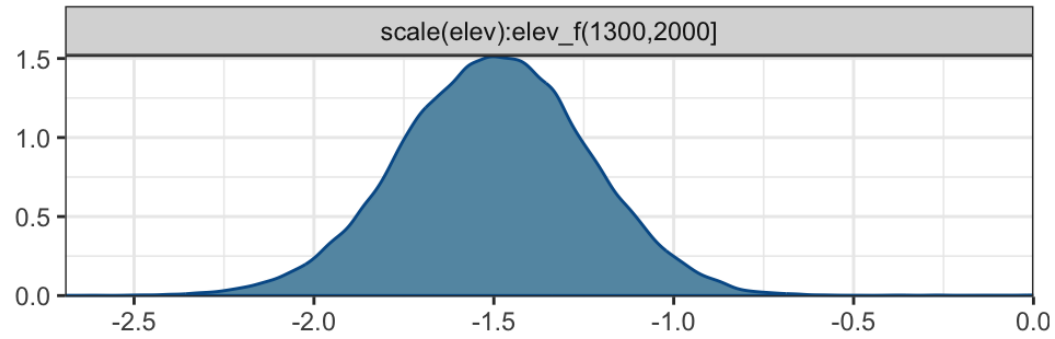
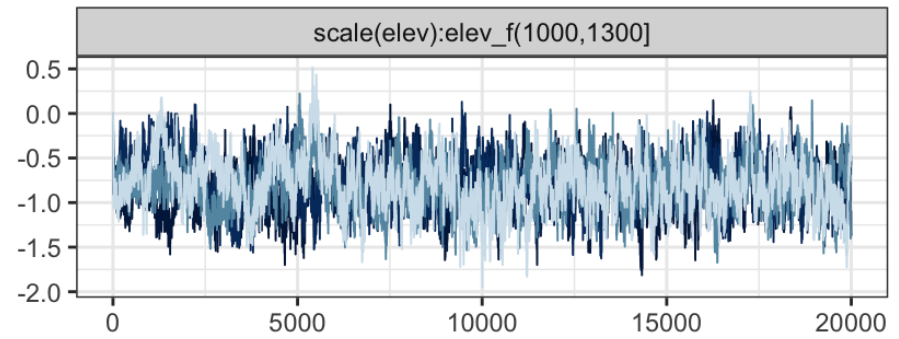
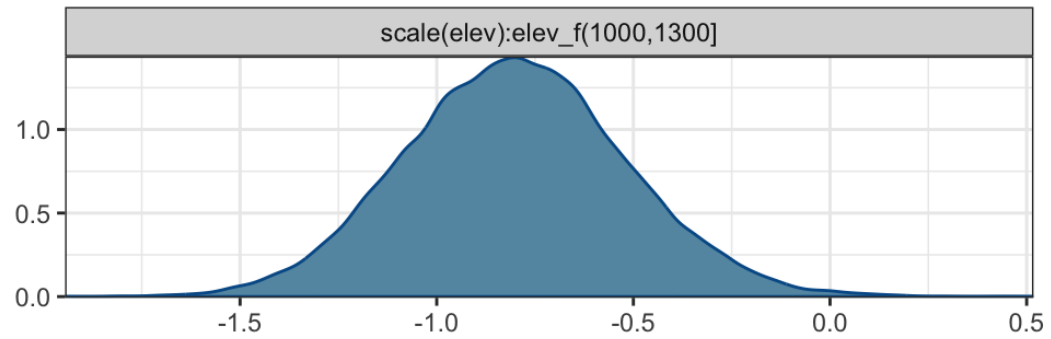
# Diagnostics

```
1 plot(ll_gp, vars=1:3)
```



Chain  
— 1  
— 2  
— 3  
— 4

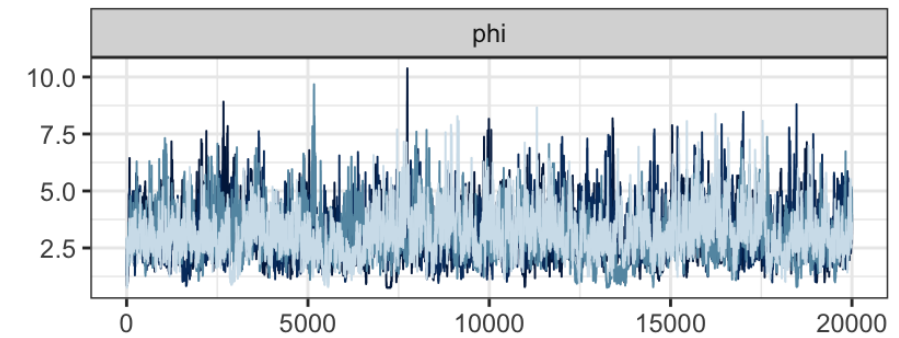
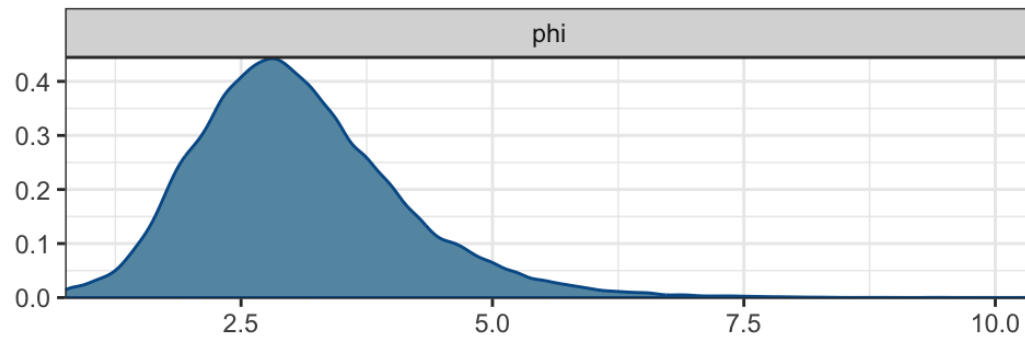
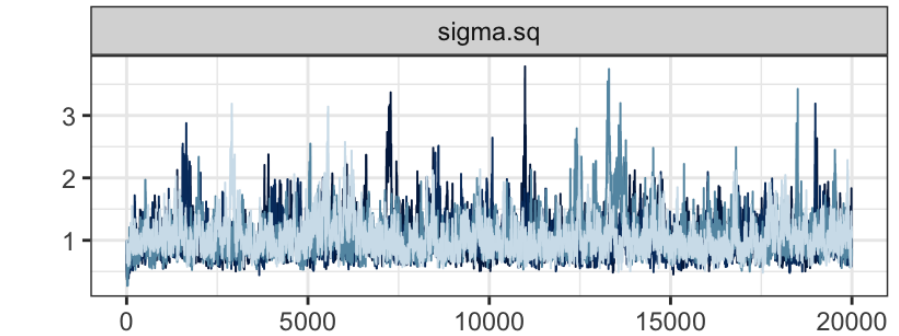
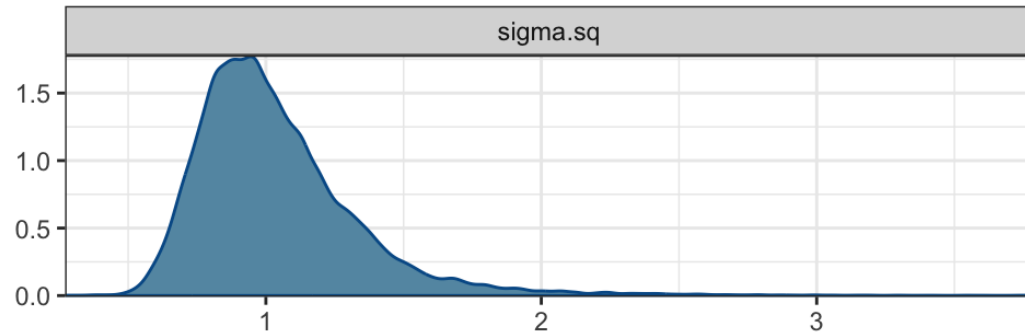
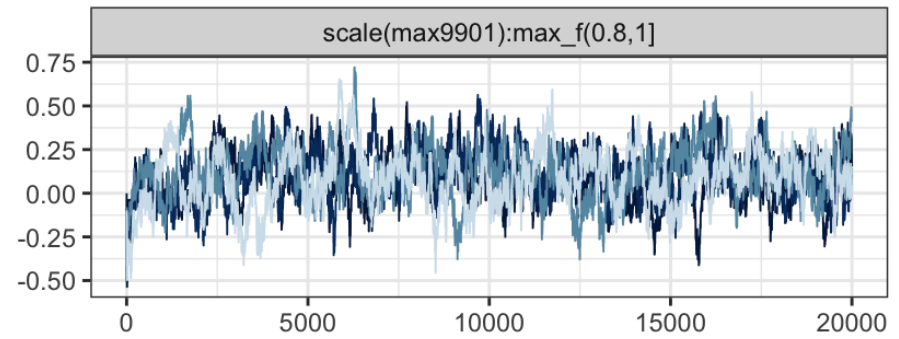
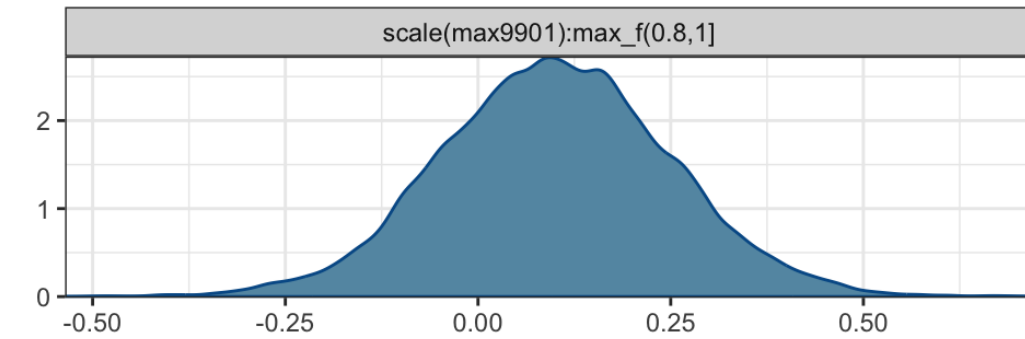
```
1 plot(ll_gp, vars=4:6)
```



Chain  
— 1  
— 2  
— 3  
— 4



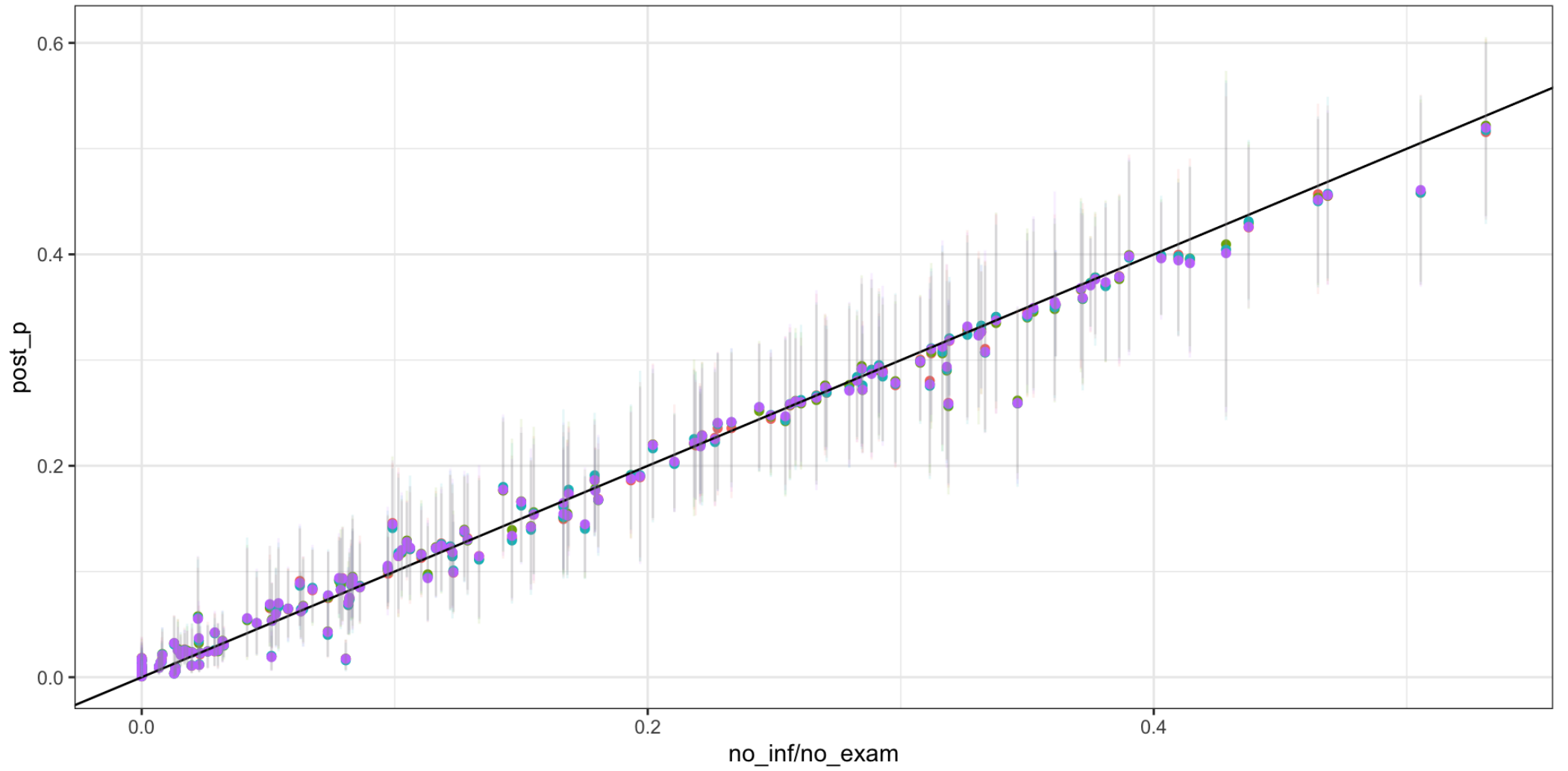
```
1 plot(ll_gp, vars=7:9)
```



Chain  
— 1  
— 2  
— 3  
— 4

# Prediction (training)

```
1 ll_gp_pred = predict(  
2   ll_gp,  
3   newdata=loaloe,  
4   coords = c("longitude", "latitude"),  
5   thin = 25,  
6   verbose=FALSE  
7 )  
8  
9 ll_gp_pred_y = tidybayes::gather_draws(ll_gp_pred, y[i]) %>%  
10  group_by(.chain, i) %>%  
11  summarize(  
12    post_p = mean(.value),  
13    q025 = quantile(.value, 0.025),  
14    q975 = quantile(.value, 0.975)  
15 )
```



# Prediction - Testing

```
1 ll_gp_test_pred = predict(  
2   ll_gp,  
3   newdata=loaloe_test,  
4   coords = c("longitude", "latitude"),  
5   thin = 25,  
6   verbose=FALSE  
7 )  
8  
9 ll_gp_test_pred_y = tidybayes::gather_draws(ll_gp_test_pred, y[i]) %>%  
10  group_by(.chain, i) %>%  
11  summarize(  
12    post_p = mean(.value),  
13    q025 = quantile(.value, 0.025),  
14    q975 = quantile(.value, 0.975)  
15 )
```



# Diggle's Predictive Surface

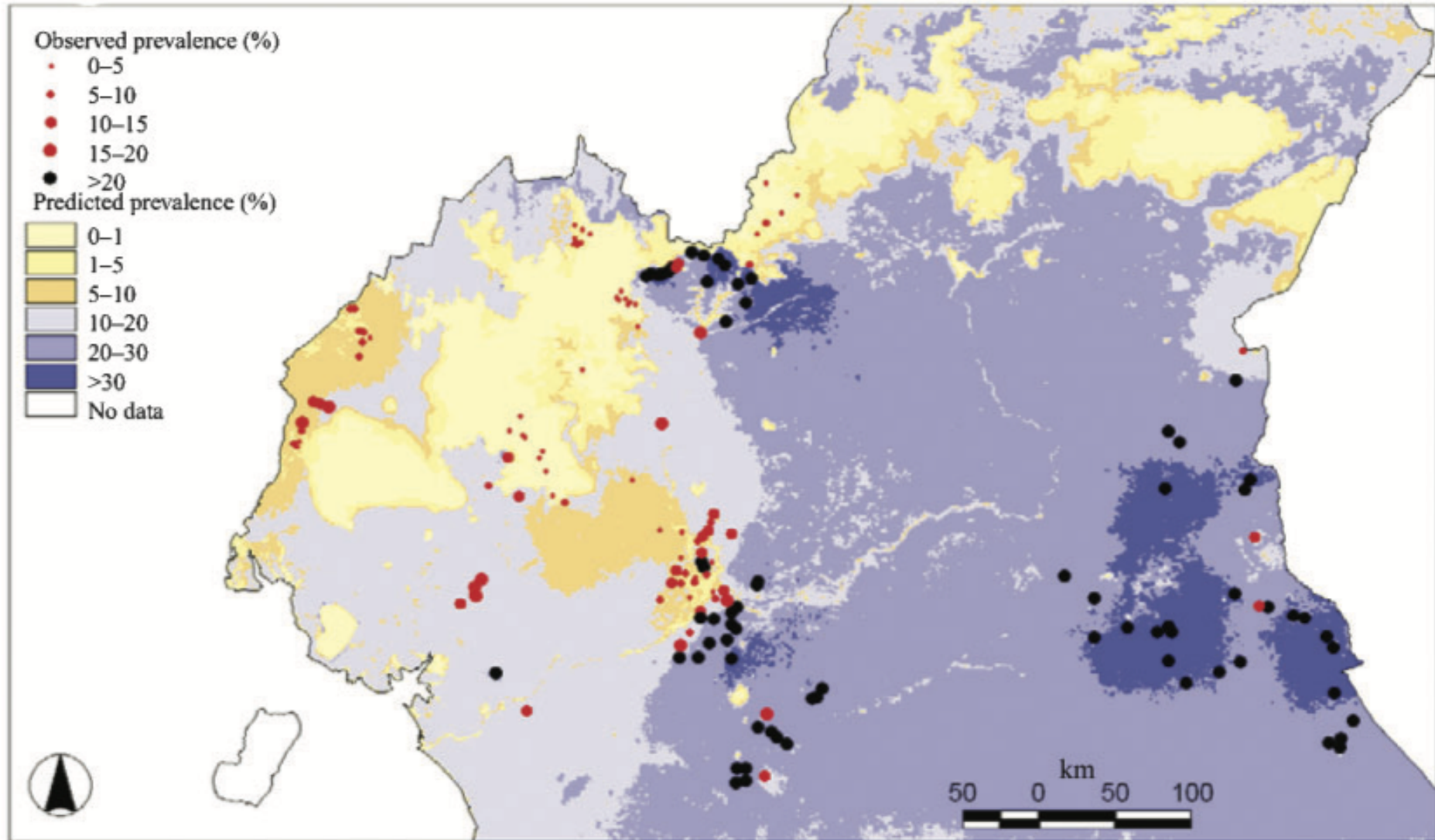
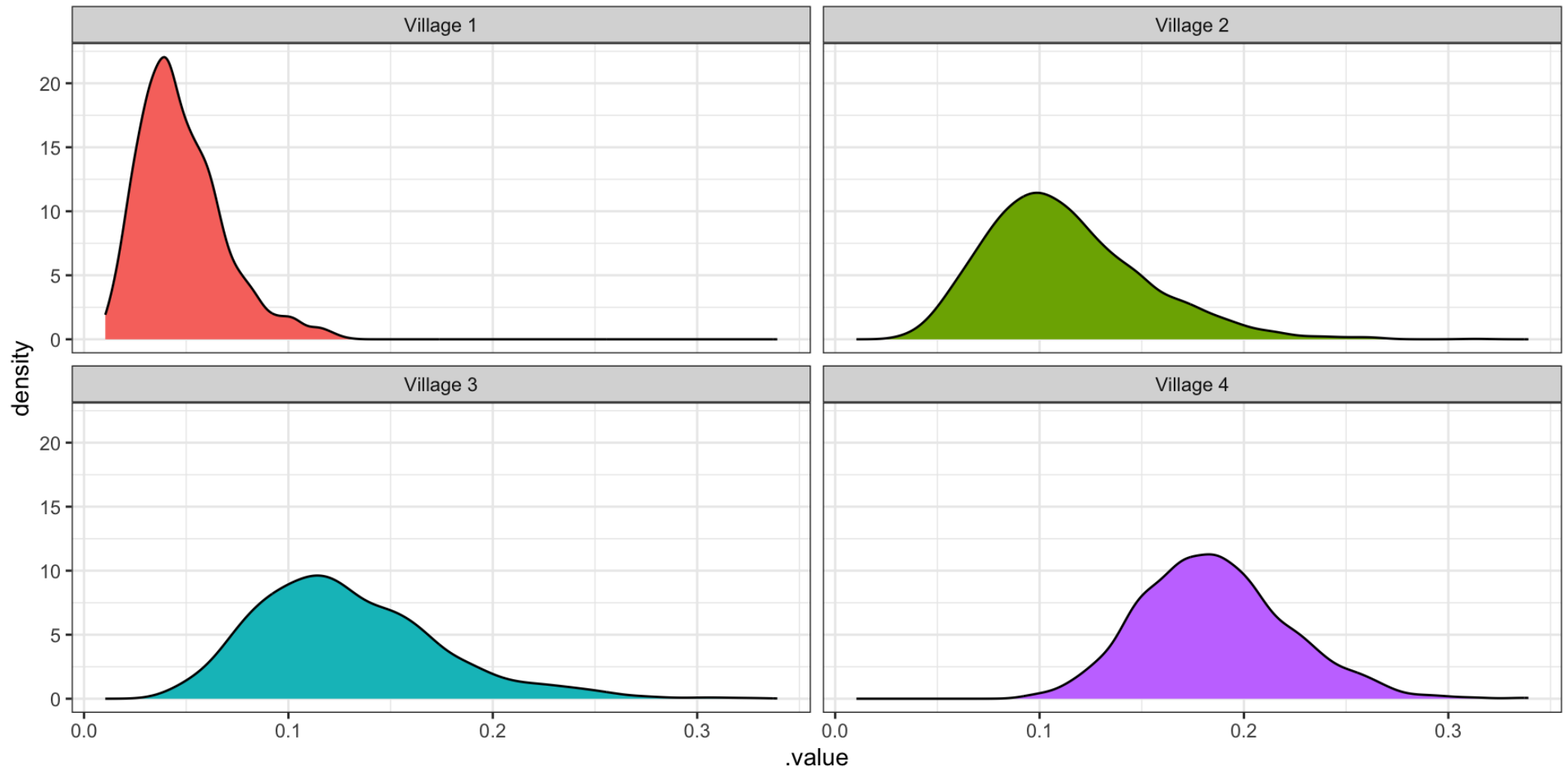


FIG. 2. Point estimates of the prevalence of *Loa loa* microfilaraemia, over-laid with the prevalences observed in field studies.

# Exceedance Probability



# Exceedance Probability Predictive Surface

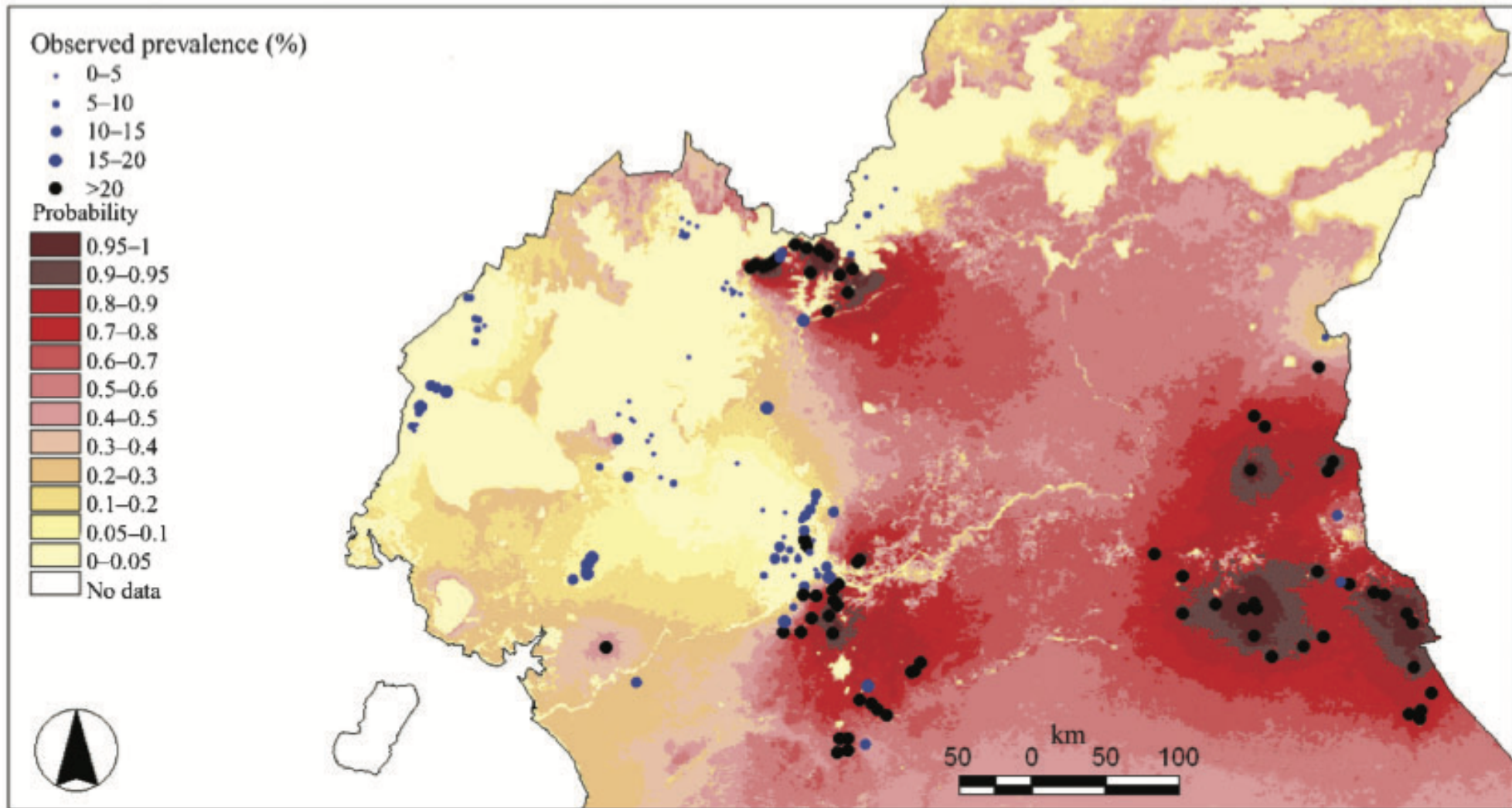


FIG. 4. A probability contour map, indicating the probability that the prevalence of *Loa loa* microfilaraemia in each area exceeds 20%, over-laid with the prevalences observed in field studies.



# Spatial Assignment of Migratory Birds

# Background

Using intrinsic markers (genetic and isotopic signals) for the purpose of inferring migratory connectivity.

- Existing methods are too coarse for most applications
- Large amounts of data are available ( 150,000 feather samples from 500 species)
- Genetic assignment methods are based on Wasser, et al. (2004)
- Isotopic assignment methods are based on Wunder, et al. (2005)

# Data - DNA microsatellites and $\delta^2\text{H}$

**Hermit Thrush**  
**(*Catharus guttatus*)**

**Wilson's Warbler**  
**(*Wilsonia pusilla*)**

138 individuals

163 individuals

14 locations

8 locations

6 loci

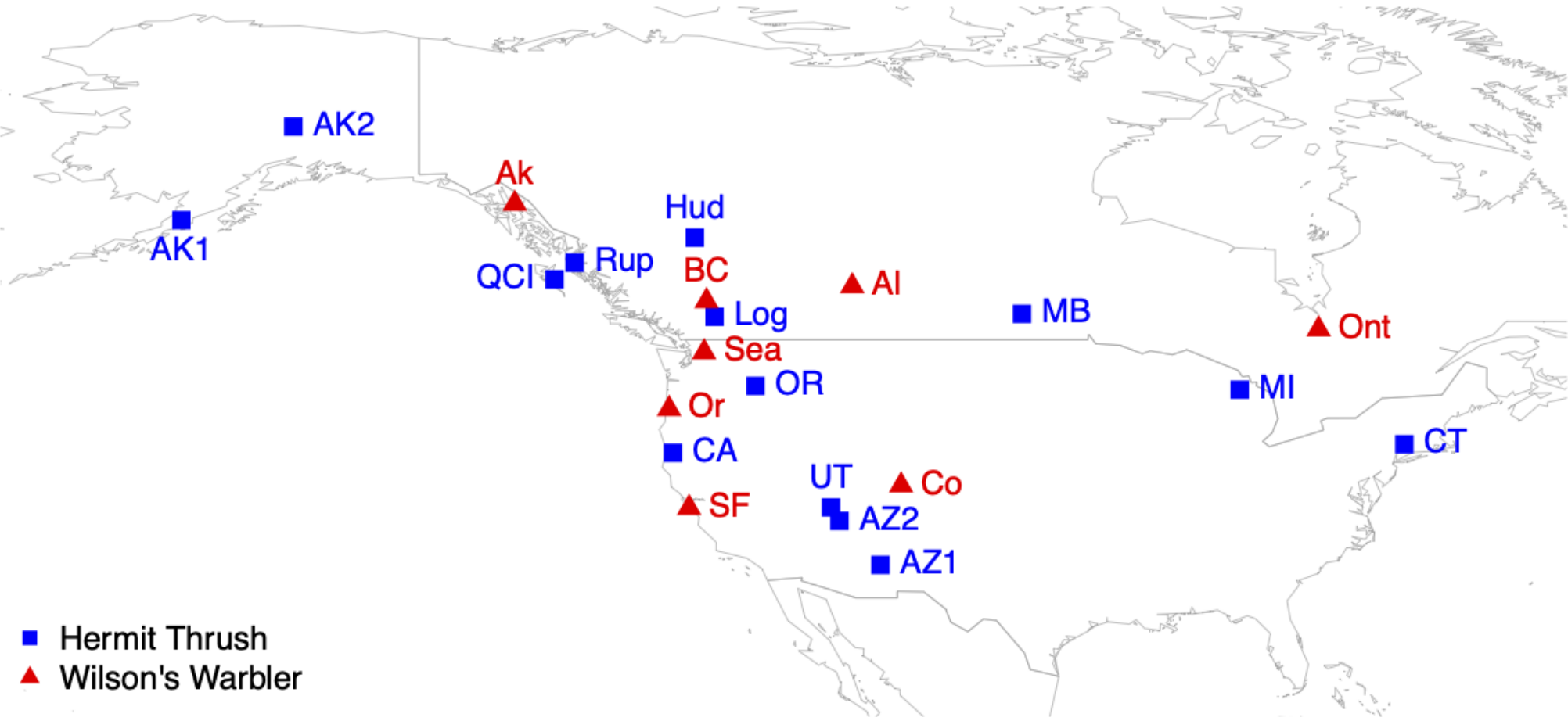
9 loci

9-27 alleles / locus

15-31 alleles / locus



# Sampling Locations



# Allele Frequency Model

For the allele  $i$ , from locus  $l$ , at location  $k$

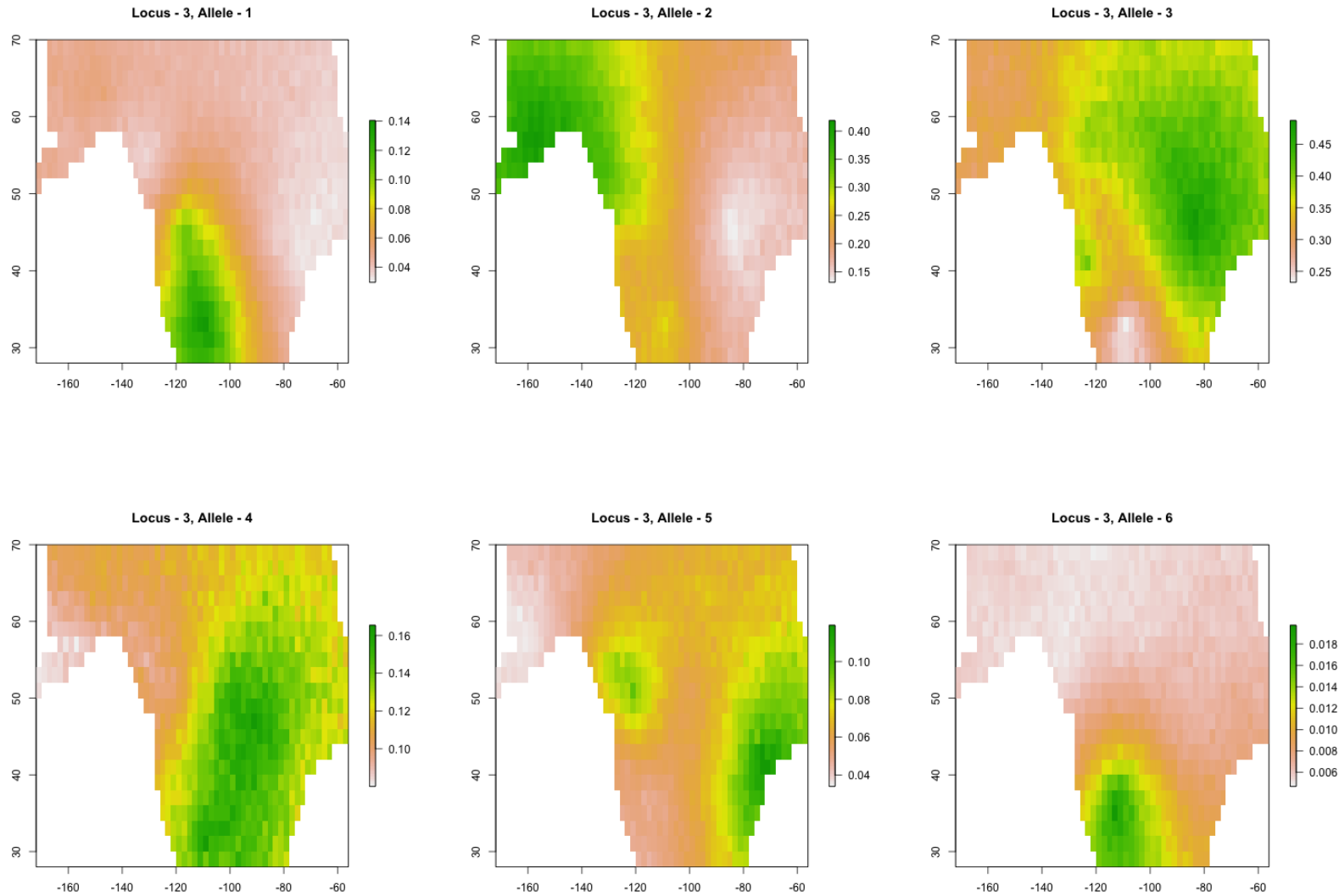
$$y_{\cdot lk} | \Theta \sim \left( \sum_i y_{ilk}, f_{\cdot lk} \right)$$

$$f_{ilk} = \frac{\exp(\Theta_{ilk})}{\sum_i \exp(\Theta_{ilk})}$$

$$\Theta_{il} | \alpha, \mu \sim (\mu_{il}, \Sigma)$$

$$\{\Sigma\}_{ij} = \sigma^2 \exp \left( - (\{d\}_{ij} r)^\psi \right) + \sigma_n^2 \mathbb{1}_{i=j}$$

# Predictions by Allele (Locus 3)



# Genetic Assignment Model

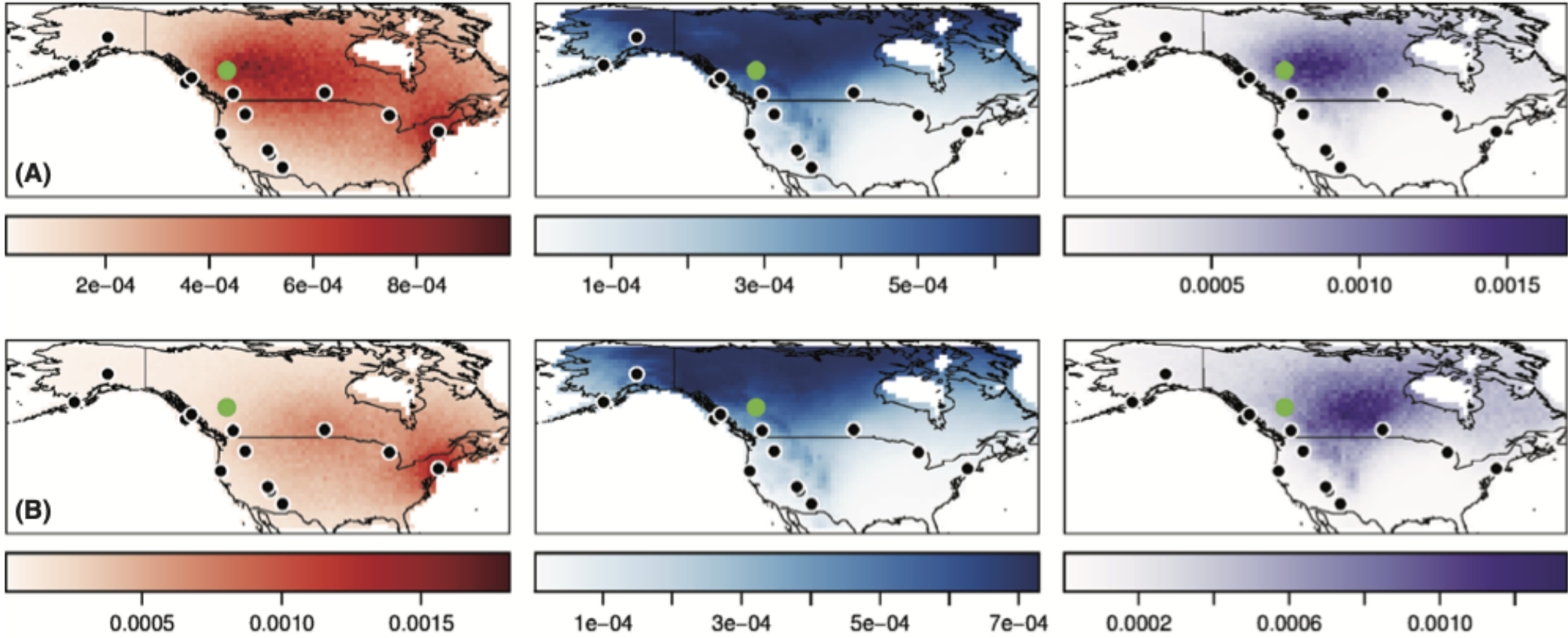
Assignment model assuming Hardy-Weinberg equilibrium and allowing for genotyping ( $\delta$ ) and single amplification ( $\gamma$ ) errors.

$$P(S_G | \mathbf{f}, k) = \prod_1 P(i_1, j_1 | \mathbf{f}, k)$$

$$P(i_1, j_1 | \mathbf{f}, k) = \begin{cases} \gamma P(i_1 | \mathbf{f}, k) + (1 - \gamma) P(i_1 | \tilde{\mathbf{f}}, k)^2 & \text{if } i = j \\ (1 - \gamma) P(i_1 | \mathbf{f}, k) P(j_1 | \mathbf{f}, k) & \text{if } i \neq j \end{cases}$$

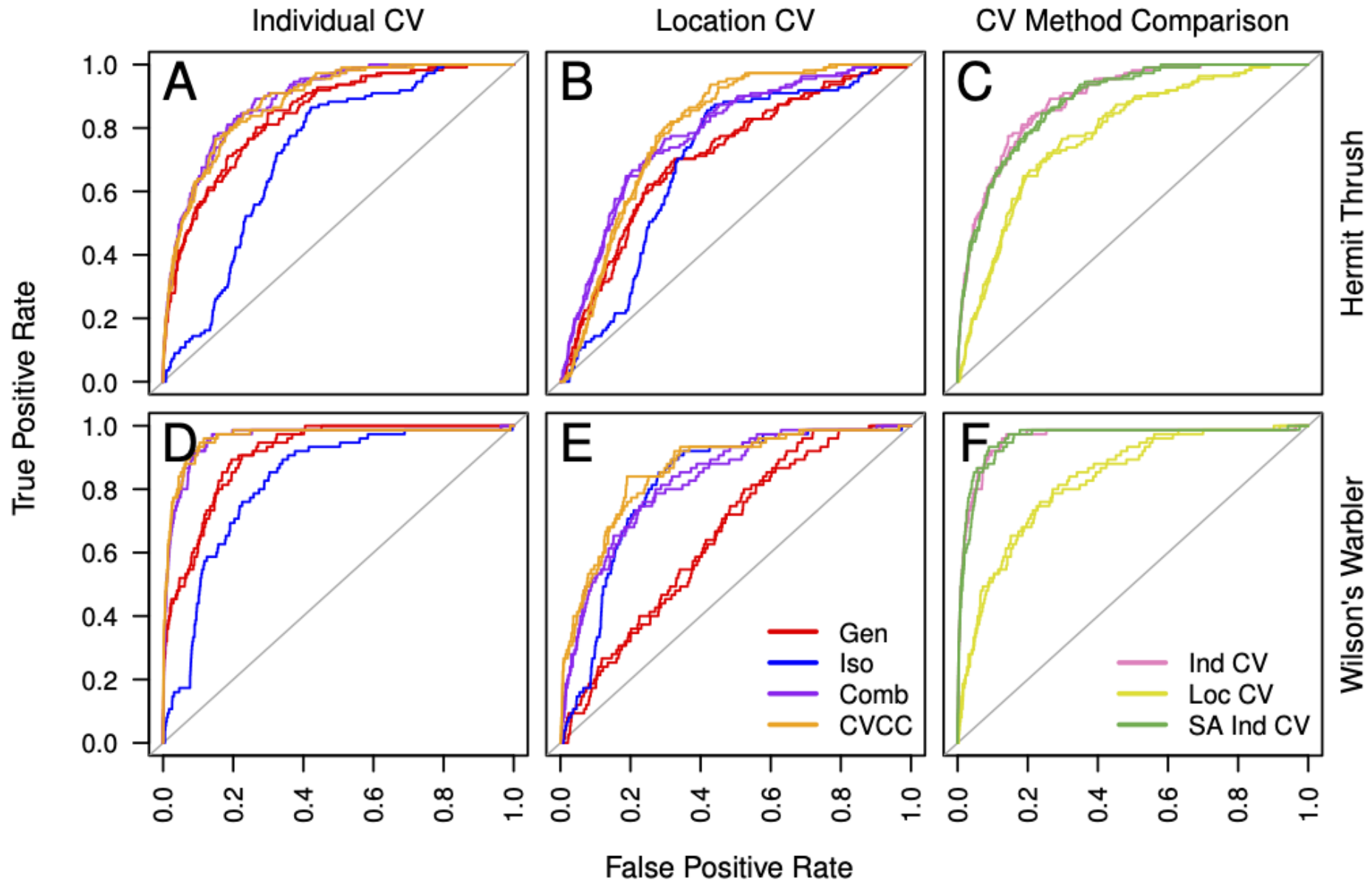
$$P(i_1 | \mathbf{f}, k) = (1 - \delta) f_{i_1 k} + \delta / m_1$$

# Combined Model

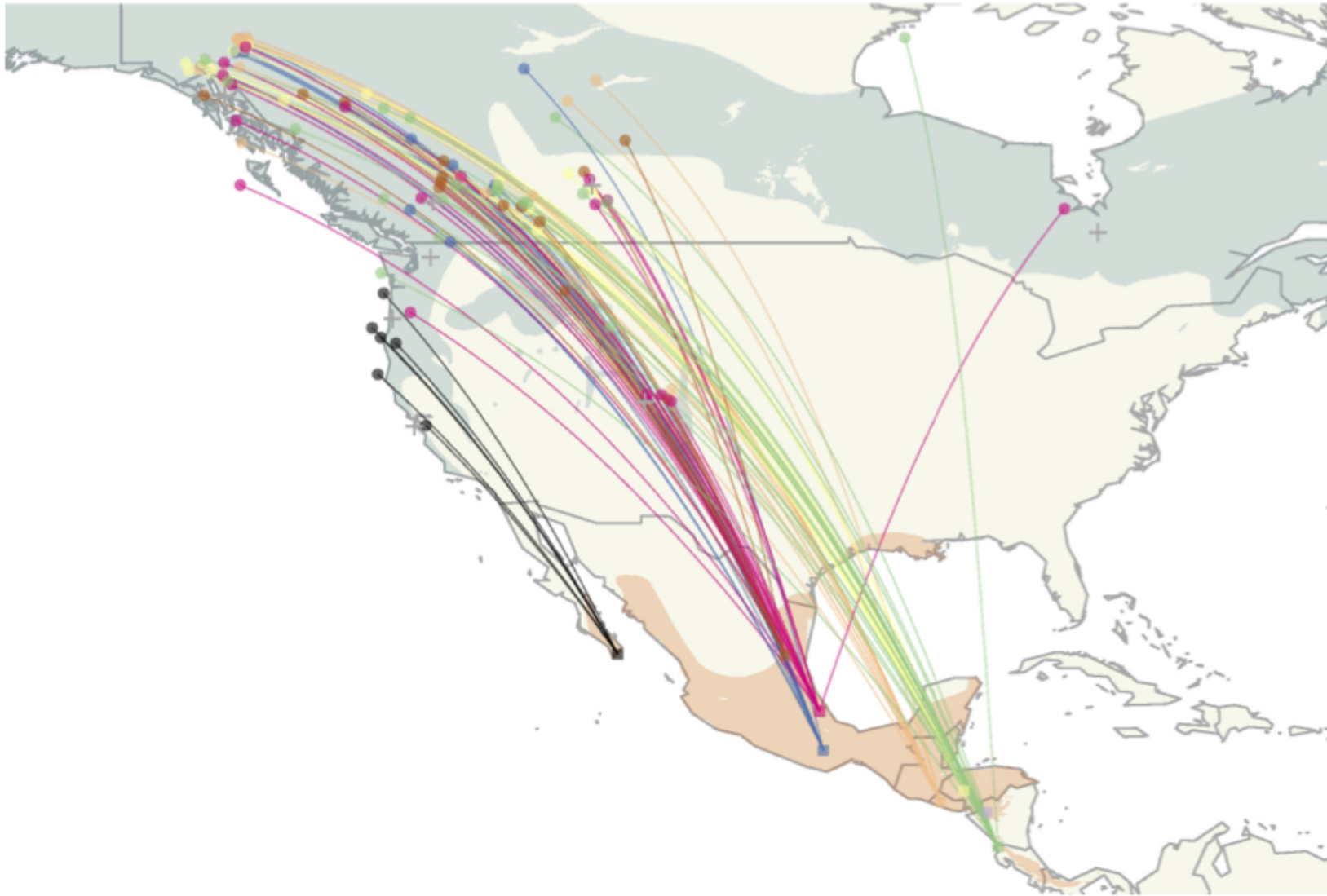




# Model Assessment



# Migratory Connectivity



Sta 344 - Fall 2022